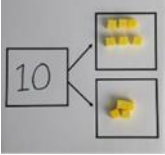
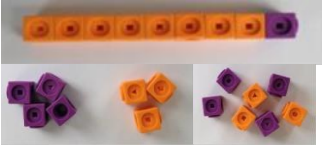
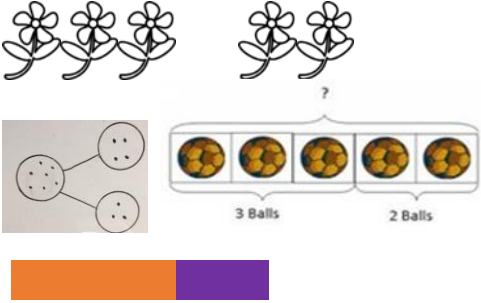
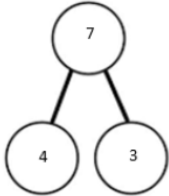
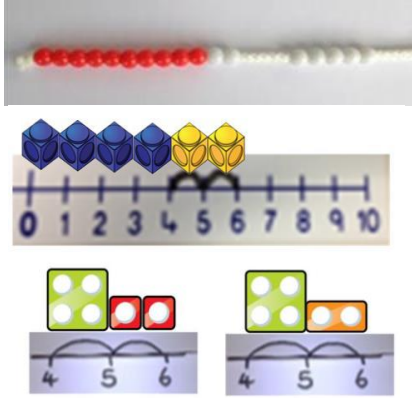
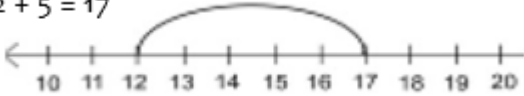
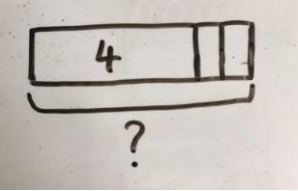
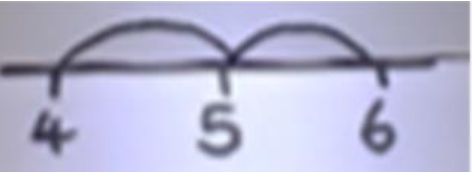


# Wrenbury Primary School calculation policy

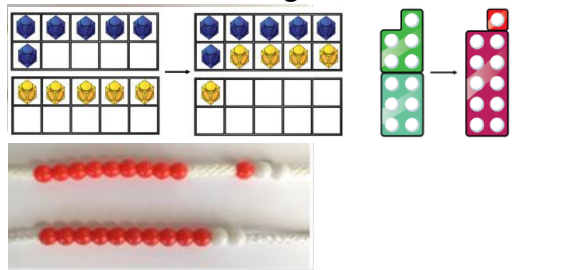
(adapted from the White Rose Maths Hub calculation policy, this is a working document and will be amended as necessary)

## Addition

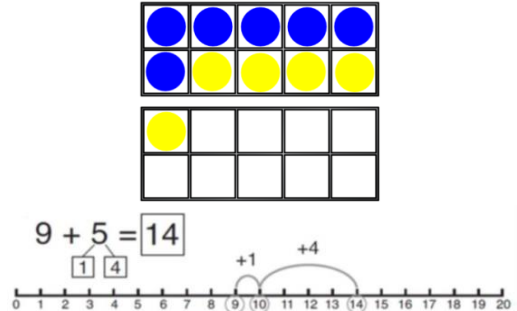
Objective	Concrete	Pictorial	Abstract
<p>Combining two parts to make a whole: part – part whole model</p>	<p>Use part – part whole model.</p>  <p>Use cubes to add two numbers together as a group of in a bar</p> 	<p>Use pictures to add two numbers together as a group or in a bar</p> 	<p>Use the part – part whole diagrams shown below to move into the abstract</p> <p><math>4 + 3 = 7</math> Four is a part, 3 is a part and the whole is 7</p> 
<p>Counting on from the biggest number</p>	<p>Counting on using bead strings, cubes on a number line or Numicon on a number line</p> 	<p>Count on in ones along a number line starting with the biggest number</p> <p><math>12 + 5 = 17</math></p>  <p>Using a bar model to count on from the biggest number</p> 	<p>Place the larger number in your head and count on the smaller number to find your answer.</p> <p><math>5 + 12 = 17</math></p> <p>Using an abstract number line</p> 

Regrouping to make ten

Using ten frames with counters/cubes, using Numicon or bead strings



Children to draw the ten frame with counters/cubes or using a number line, regrouping or partitioning smaller number



Children to develop an understanding of equality e.g.

$$6 + \square = 11$$

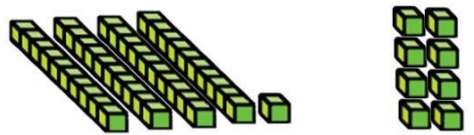
$$6 + 5 = 5 + \square$$

$$6 + 5 = \square + 4$$

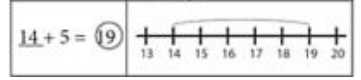
2 digit number add a one digit number (TO + O)

Develop understanding of partitioning and place value using Base 10/dienes to add

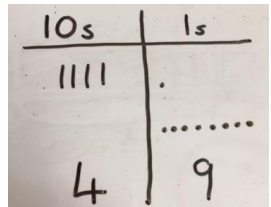
$$41 + 8$$



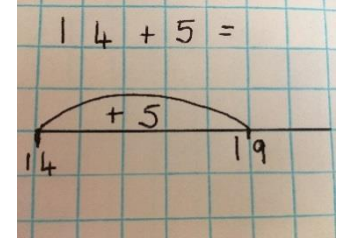
Using a number line to jump on in ones



Drawing Base 10/dienes to add on ones



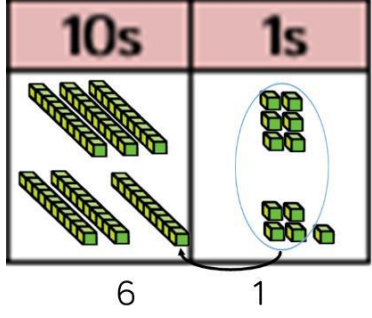
Using an abstract number line



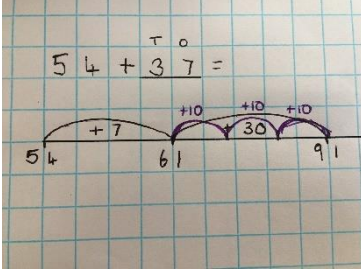
Counting on from the biggest number in your head/using your fingers to support

2 digit number add a 2 digit number (TO + TO)

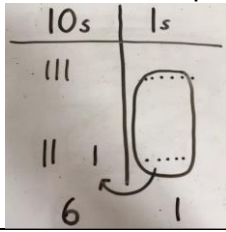
Develop understanding of partitioning and place value using Base 10/dienes to add



Adding ones and tens on a number line



Represent Base 10/dienes in a place value chart



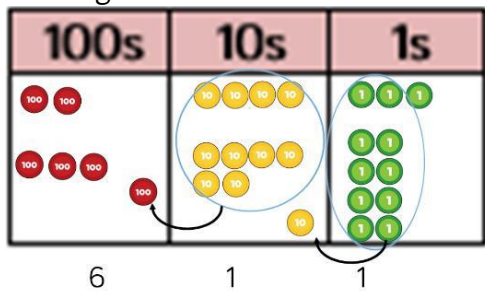
Using an abstract number line

Formal method (if appropriate)

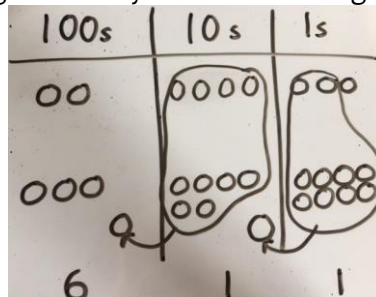
$$\begin{array}{r} 36 \\ +25 \\ \hline 61 \\ 1 \end{array}$$

3 digit number  
add 2  
digit/3/digit  
etc. numbers  
(HTO +  
TO/HTO)

Using Base 10/dienes to further develop an understanding of addition. Where there are 10 ones in the 1s column, we exchange them for 1 ten, when there are 10 tens in the 10s column, we exchange them for 1 hundred.



Represent counters in a place value chart, showing when they make an exchange

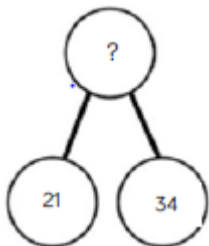


Formal written method

$$\begin{array}{r} 243 \\ +368 \\ \hline 611 \\ \hline 11 \end{array}$$

**Conceptual variation; different ways to ask children to solve 21 + 34**

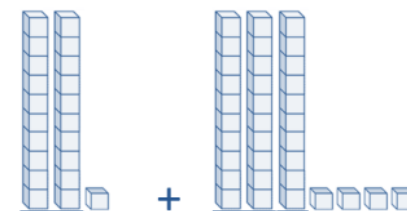
?	
21	34



Word problems:  
In year 3, there are 21 children and  
in year 4, there are 34 children.  
How many children in total?  
 $21 + 34 = 55$ . Prove it

$$\begin{array}{r} 21 \\ +34 \\ \hline \end{array}$$

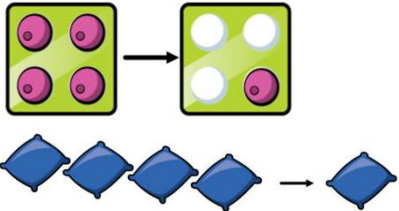
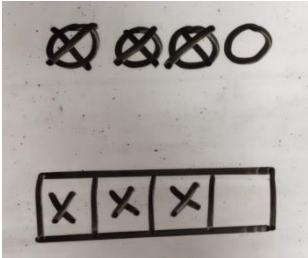
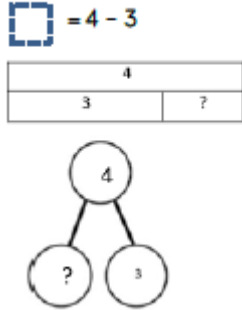
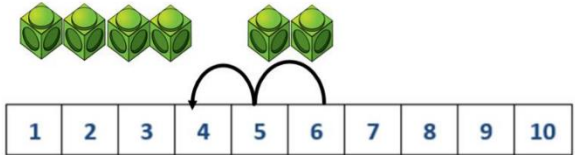

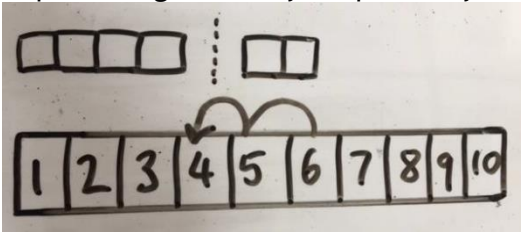
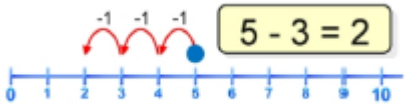
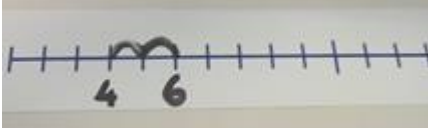
$21 + 34 =$   
 $\square = 21 + 34$   
Calculate the sum of twenty-one and thirty-four.

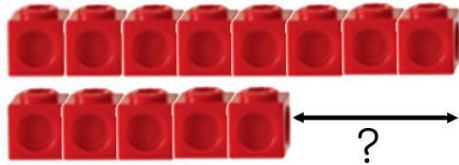
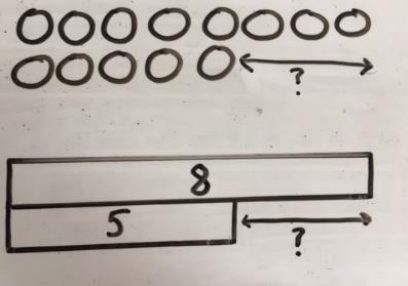
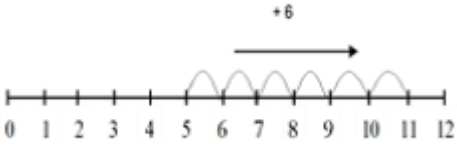
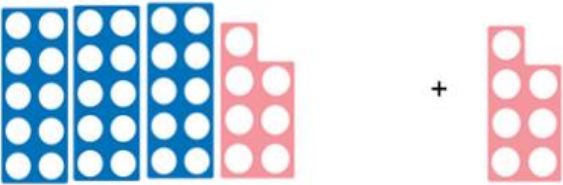
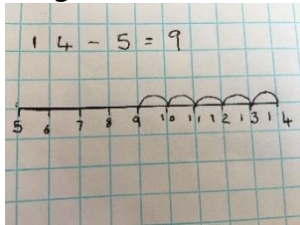
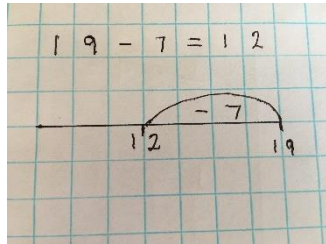
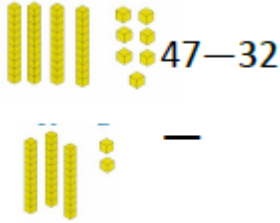
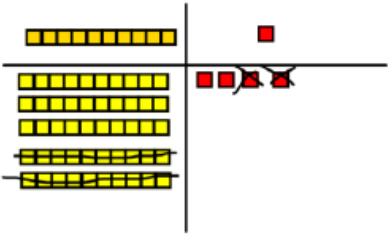
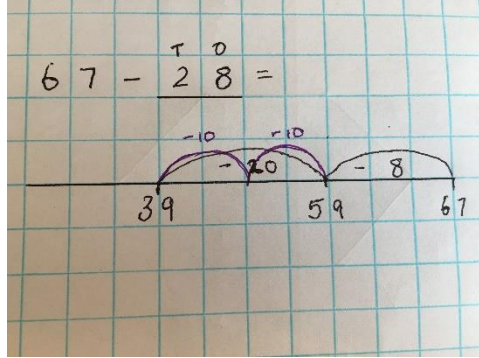


Missing digit problems

10s	1s
10 10	1
10 10 10	?
?	5

## Subtraction

Objective	Concrete	Pictorial	Abstract
<p>Subtraction as taking away</p>	<p>Physically taking away and removing objects from a whole (tens frames, Numicon, cubes and other items such as bean bags)</p> <p><math>4 - 3 = 1</math></p> 	<p>Drawing the concrete resources they are using and cross out the correct amount. The bar model can also be used.</p> 	<p>Using numbers within part, part whole models or bar models.</p> <p><math>4 - 3 =</math></p> 
<p>Subtraction as counting back</p>	<p>Counting Back from the biggest number (using number lines or number tracks)</p> <p>Children start with 6 and count back 2</p> <p><math>6 - 2 = 4</math></p>  <p>Moving the beads along the bead string as you count backwards</p> 	<p>Representing what they see pictorially</p>  <p>Counting back on a number lines</p> 	<p>Counting back on a blank number line or counting back in their heads (using fingers if necessary)</p> 
<p>The difference between two amounts</p>	<p>Finding the difference (using cubes, Numicon, Cuisenaire rods or another appropriate resource)</p>	<p>Children to draw cubes/concrete objects or use the bar model to illustrate what they need to calculate</p>	<p>Find the difference between 8 and 5 – children to understand that finding the difference is the same as taking away and therefore using counting back methods to find the answer.</p>

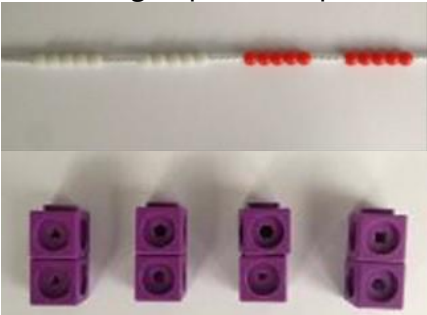
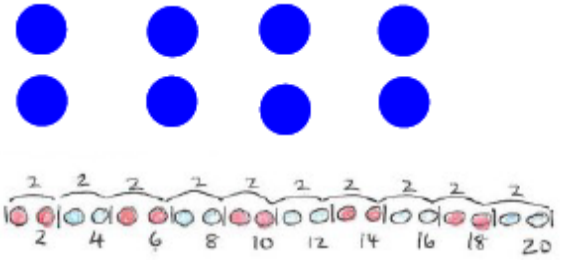
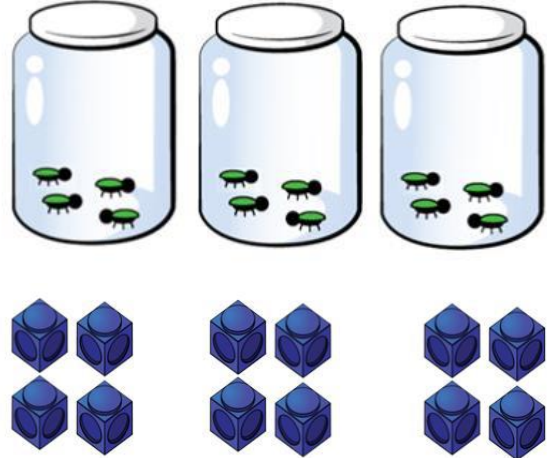
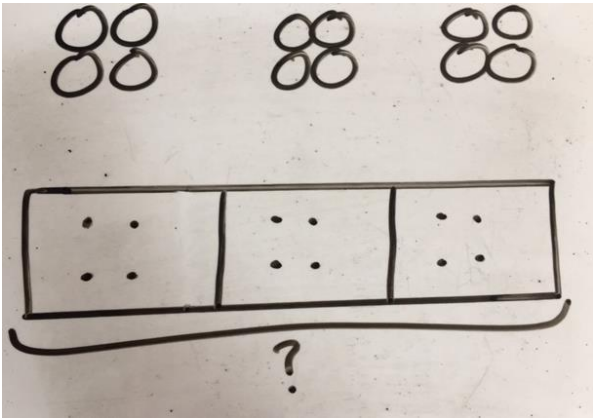
	<p>Calculate the difference between 8 and 5</p> 	 <p>Count on using a number line to find the difference</p> 	
<p>2 digit number subtract a 1 digit number</p>	<p>Using Numicon to create a 2-digit number and adding on the 1-digit number to find the total <math>37 + 7</math></p> 	<p>Count back using a number line</p> 	<p>Abstract number line</p>  <p>Count back from the biggest number</p>
<p>2 digit number subtract a 2 digit number</p>	 <p>Use base 10 or Numicon to model</p> <p>Column method using base 10 and having to exchange.</p> <p><math>41 - 26</math></p>	<p>Draw representations to support understanding</p>  <p>Calculations</p> $\begin{array}{r} 54 \\ - 22 \\ \hline 32 \end{array}$	<p>Subtract ones and tens using an abstract number line</p> 

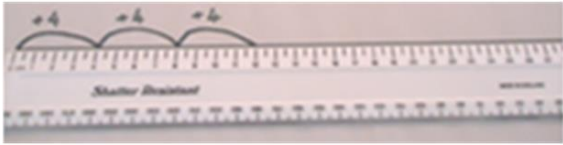


Subtracting 3 digit numbers and 2 digit numbers etc.	<p>Column methods using place value counters or base 10/dienes</p> <p>234 - 88</p>	<p>Represent the place value counters or base 10/dienes pictorially, showing what has been exchanged</p>	<p>Formal column method. Children must understand what has happened when they have crossed out digits</p> $\begin{array}{r} \phantom{2}^2 \phantom{3}^1 4 \\ - 88 \\ \hline 6 \end{array}$

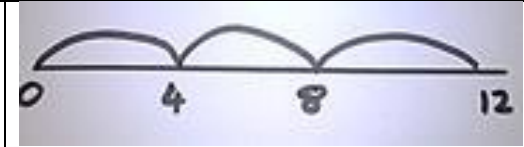
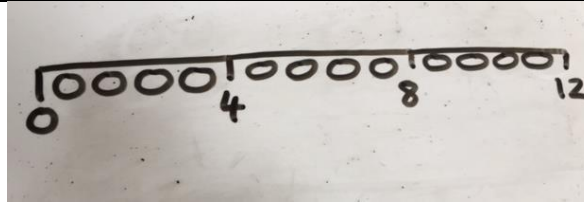
<b>Conceptual variation; different ways to ask children to solve 391 - 186</b>			
	<p>Raj spent £391, Timmy spent £186. How much more did Raj spend? Calculate the difference between 391 and 186.</p>	$\square = 391 - 186$ $\begin{array}{r} 391 \\ -186 \\ \hline \end{array}$ <p>What is 186 less than 391?</p>	<p>Missing digit calculations</p> $\begin{array}{r} 39\square \\ - \square\square 6 \\ \hline \square 0 5 \end{array}$

## Multiplication

Objective	Concrete	Pictorial	Abstract
Counting in multiples	Count the groups of multiples 	Draw representations for counting in multiples 	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
Multiplication as repeated addition $3 \times 4$ $4 + 4 + 4$ There are 3 equal groups, with 4 in each group		Represent practical resources in a picture and use a bar model 	$3 \times 4 = 12$  $4 + 4 + 4 = 12$
Multiplication as repeated groups	Number lines to show repeated groups $3 \times 4$	Represent this pictorially alongside a number line	Abstract number line showing three jumps of 4  $3 \times 4 = 12$

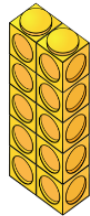


Cuisenaire rods can be used too

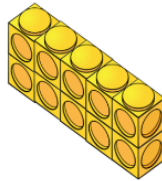


Show that multiplication of two numbers can be done in any order (commutative)

Use arrays to illustrate commutativity, counters and other objects can be used

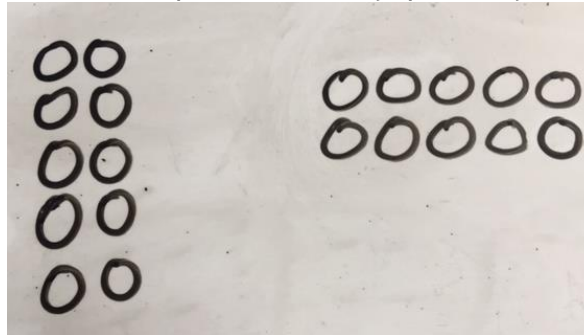


2 lots of 5



5 lots of 2

Children to represent the arrays pictorially



Children to be able to use an array to write a range of calculations

$$10 = 2 \times 5$$

$$5 \times 2 = 10$$

$$2 + 2 + 2 + 2 + 2 = 10$$

$$10 = 5 + 5$$

Multiplying a 2 digit number by a 1 digit number

Formal column method to multiply a 2-digit number by a 1-digit number using place value counters/dienes

$$3 \times 23$$

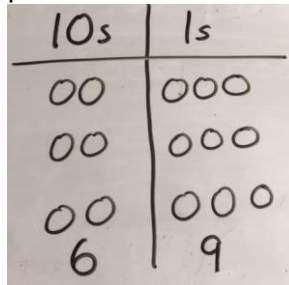


6

9

$$6 \times 23$$

Represent the column method by drawing place value counters



$$6 \times 23$$

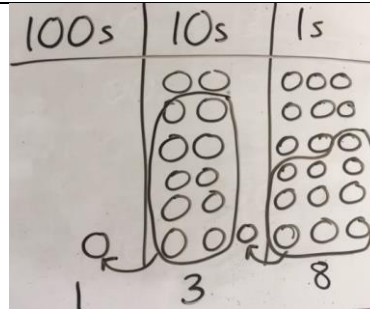
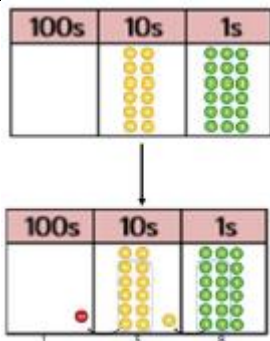
Record multiplication process step by step through partitioning or column method

$$3 \times 23 \quad \begin{array}{l} 3 \times 20 = 60 \\ 3 \times 3 = 9 \\ 60 + 9 = 69 \end{array}$$

$$\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$$

$$6 \times 23$$





$$6 \times 23 =$$

$$\begin{array}{r} 23 \\ \times 6 \\ \hline 138 \\ 11 \end{array}$$

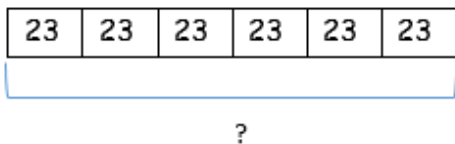
Multiply 3d x 3d or 4d x 2d etc.

When children start to multiply 3d x 3d and 4d x 2d etc., they should be confident with the abstract methods

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \\ 11 \end{array}$$

Answer: 3224

**Conceptual variation; different ways to ask children to solve 6 x 23**



Mai had to swim 23 lengths, 6 times a week.  
How many lengths did she swim in one week?  
With the counters, prove that  $6 \times 23 = 138$

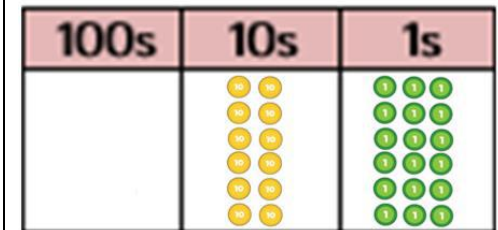
Find the product of 6 and 23

$$6 \times 23 =$$

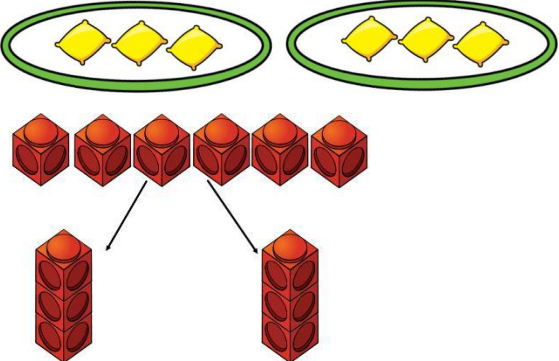
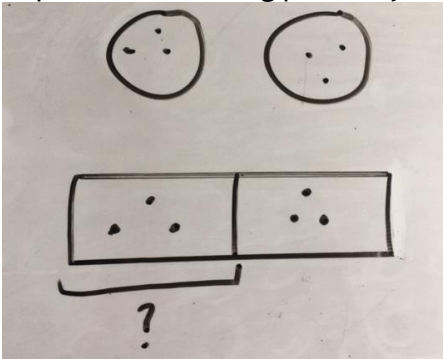
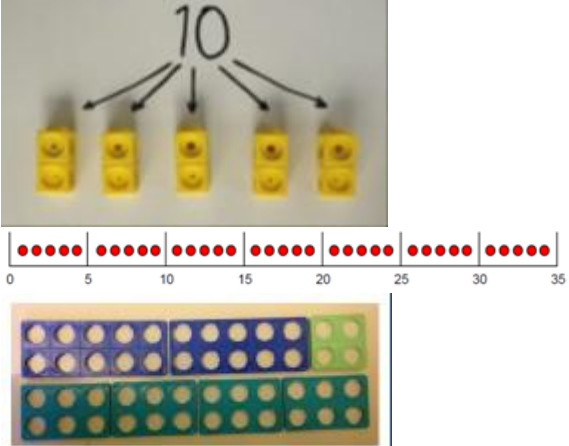
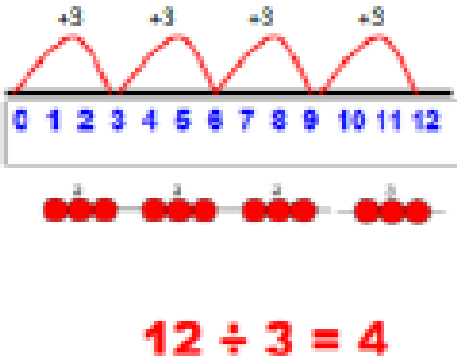
$$\square = 6 \times 23$$



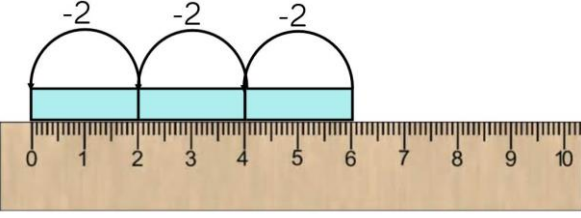
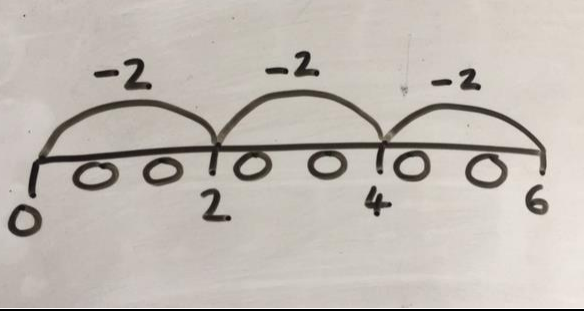
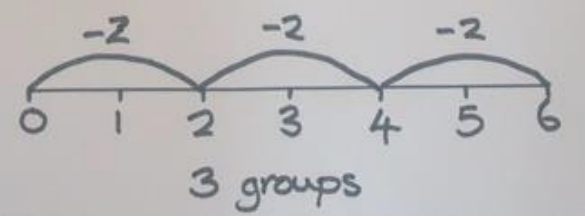
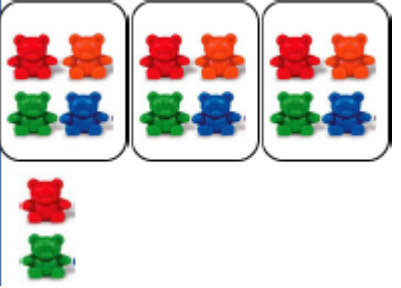



$$\begin{array}{r} 6 \quad 23 \\ \times 23 \quad \times 6 \\ \hline \quad \quad \end{array}$$

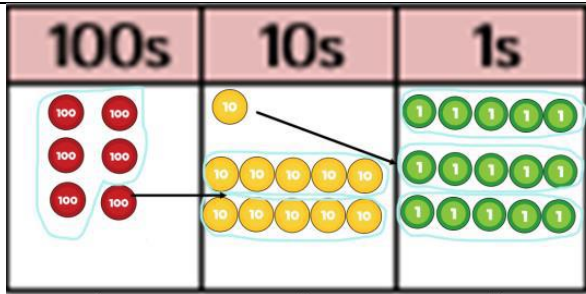
What is the calculation?  
What is the product?



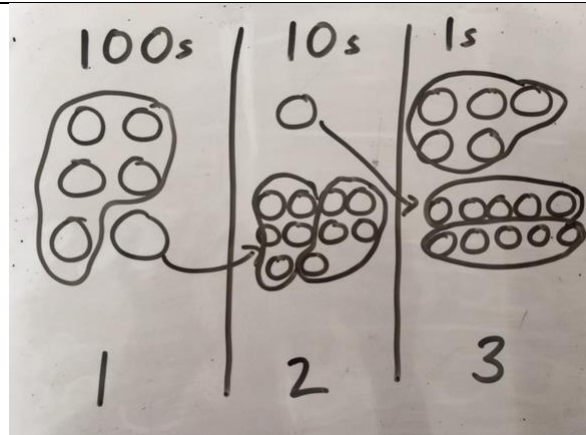
## Division

Objective	Concrete	Pictorial	Abstract		
<p>Division by sharing</p>	<p>Sharing using a range of objects <math>6 \div 2</math></p> 	<p>Represent the sharing pictorially</p> 	<p>Using bars to represent sharing <math>6 \div 2 = 3</math></p> <table border="1" data-bbox="1550 320 2130 408" style="width: 100%; text-align: center;"> <tr> <td style="width: 50%; height: 50px;">3</td> <td style="width: 50%; height: 50px;">3</td> </tr> </table> <p>Children should be encouraged to use their 2 times tables facts.</p>	3	3
3	3				
<p>Division as grouping</p>	<p>Dividing quantities into equal groups Use cubes, counters, Numicon, objects or place value counters to support understanding</p> 	<p>Use number lines for grouping</p>  <p style="text-align: center; color: red; font-size: 1.2em;"><math>12 \div 3 = 4</math></p> <p>Using a bar model to divide the bar into equal groups</p>	<p><math>28 \div 7 = 4</math> Divide 28 into 7 groups. How many are in each group?</p> <p>How many groups of 6 in 24? <math>24 \div 6 = 4</math></p>		

	$96 \div 3 = 32$ 	$20$  $20 \div 5 = ?$ $5 \times ? = 20$	
Division with repeated subtraction	Repeated subtraction using Cuisenaire rods above a ruler  3 groups of 2	Represent the repeated subtraction pictorially 	Abstract number line to represent the equal groups that have been subtracted 
Division with remainders	Divide objects between groups to see how much is left over $14 \div 3$ 	Using a number line to jump forwards in equal jumps and see how many more you need to jump to find the remainder  Draw dots and group them to divide amount and clearly show the remainder 	Complete written divisions and show the remainder using r $29 \div 8 = 3 \text{ REMAINDER } 5$ 
Short division	Short division using place value counters to groups $615 \div 5$	Represent the place value counters pictorially	Children to do the calculation using the short division scaffold (bus stop)



1. Make 615 with place value counters.
2. How many groups of 5 hundreds can you make with 6 hundred counters?
3. Exchange 1 hundred for 10 tens.
4. How many groups of 5 tens can you make with 11 ten counters?
5. Exchange 1 ten for 10 ones.
6. How many groups of 5 ones can you make with 15 ones?



$$\begin{array}{r}
 123 \\
 5 \overline{) 615} \\
 \underline{5} \phantom{0} \\
 11 \phantom{0} \\
 \underline{10} \\
 15 \\
 \underline{15} \\
 0
 \end{array}$$

Division with remainders

$$\begin{array}{r}
 86 \text{ r } 2 \\
 5 \overline{) 432} \\
 \underline{40} \\
 32 \\
 \underline{30} \\
 2
 \end{array}$$

Division that use the decimal places

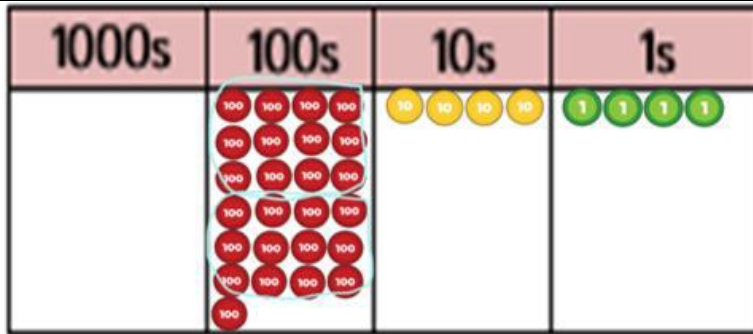
$$\begin{array}{r}
 14.6 \\
 35 \overline{) 511.0} \\
 \underline{35} \\
 16 \\
 \underline{14} \\
 21 \\
 \underline{21} \\
 0
 \end{array}$$

Long division

Long division using place value counters

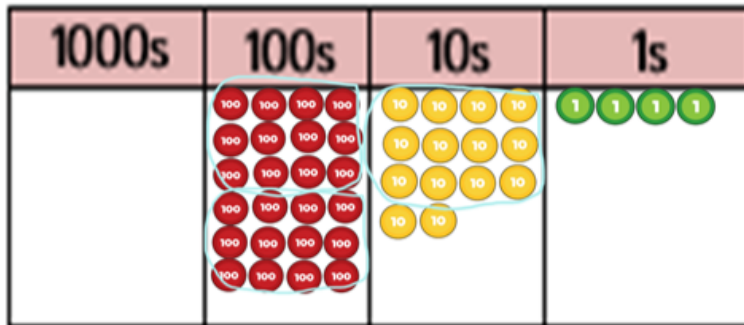


We can't group 2 thousands into groups of 12 so will exchange them.



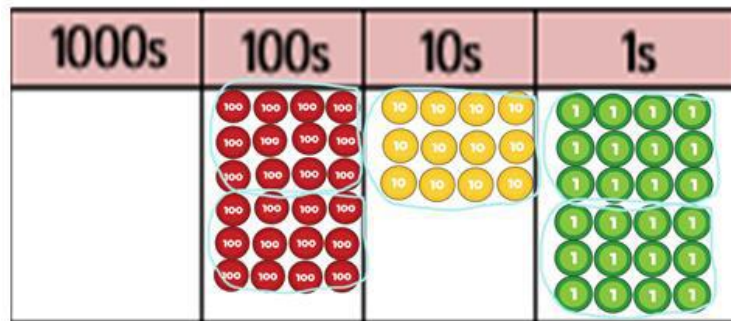
We can group 24 hundreds into groups of 12 which leaves with 1 hundred.

$$\begin{array}{r}
 02 \\
 \hline
 12 \overline{) 2544} \\
 \underline{24} \\
 1
 \end{array}$$



After exchanging the hundred, we have 14 tens. We can group 12 tens into a group of 12, which leaves 2 tens.

$$\begin{array}{r}
 021 \\
 \hline
 12 \overline{) 2544} \\
 \underline{24} \\
 14 \\
 \underline{12} \\
 2
 \end{array}$$



After exchanging the 2 tens, we have 24 ones. We can group 24 ones into 2 group of 12, which leaves no remainder.

$$\begin{array}{r}
 0212 \\
 \hline
 12 \overline{) 2544} \\
 \underline{24} \\
 14 \\
 \underline{12} \\
 24 \\
 \underline{24} \\
 0
 \end{array}$$

**Conceptual variation; different ways to ask children to solve  $615 \div 5$**

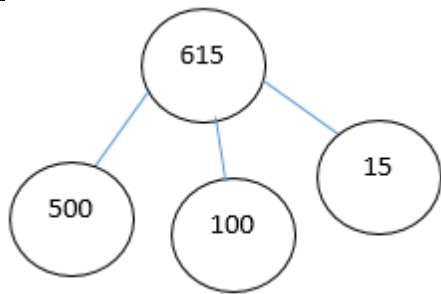
Using the part whole model below, how can you divide by 5 without using short division

I have £615 and share it equally between 5 bank accounts. How much will be in each account?

$$5 \overline{) 615}$$

What is the calculation?  
What is the answer?





615 pupils need to be put into 5 groups.  
How many will be in each group?

$$615 \div 5 =$$
$$\underline{\quad} = 615 \div 5$$

100s	10s	1s
		